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APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY
B.Tech Degree S7 (R,S) Examination November 2025 (2019 Scheme).

Course Code: ECT453

Course Name: ERROR CONTROL CODES

Max. Marks: 100

Duration: 3 Hours

PART A

Answer all questions, each carries 3 marks.

Marks

- 1 Let the generator matrix of a LBC is given as $\begin{bmatrix} 1 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 1 \end{bmatrix}$. Find the Dual code for any 2 bit message. (3)
- 2 A linear code C has parameters $(n,k,d) = (6,3,d)$ (3)
 - a. What is the possible value of d.
 - b. If d is maximum, what kind of code is C?
 - c. How many errors can be corrected and detected?
- 3 State the properties of cyclic codes. (3)
- 4 Construct generator matrix for $(7,4)$ cyclic code $g(x) = 1+x+x^3$. (3)
- 5 Determine the parameters of q-ary RS Code over $GF(256)$ for a $d_{min}=33$. (3)
- 6 What are applications of Reed Muller codes. (3)
- 7 Draw the encoder circuit for a rate 1/3 convolutional encoder with generator sequences, $g(1) = (1\ 0\ 0)$, $g(2) = (1\ 0\ 1)$, $g(3) = (1\ 1\ 1)$. (3)
- 8 What is the purpose of puncturing in turbo codes, and how does it affect the code rate. (3)
- 9 Construct the generator matrix of G_4 used in polar codes (3)
- 10 Differentiate regular and irregular LDPC. (3)

PART B

Answer any one full question from each module, each carries 14 marks.

Module I

- 11 a) Write a short note about hamming bound. (5)
- b) Consider a $(6,3)$ LBC (9)

$$G = \begin{bmatrix} 1 & 0 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 \end{bmatrix}$$

- I. Find all codewords**
- II. Find minimum hamming weight.**
- III. Draw the encoder circuit.**

OR

- 12 a) For a (5,1) repetition code (9)
- I. Write the parity check matrix**
 - II. Evaluate the syndrome for all possible single error patterns.**
- b) Define (i) Singleton bound (ii) Gilbert-Varshamov bound (5)

Module II

- 13 a) Design an encoder for (7,4) binary cyclic code generated by $g(x) = 1+x+x^3$. Find the code vector corresponding to the message vector 1001. (9)
- b) Check whether $1+x+x^3$ is primitive, irreducible. (5)

OR

- 14 a) Design a BCH Code with block length $n=7$ and the error correcting capability $t=1$. Find the code word corresponding to the message $d=[1\ 0\ 1\ 1]$ (7)
- b) Construct the values of $GF(2^4)$ for the polynomial $1+x+x^4$ (7)

Module III

- 15 a) For a RM (1,4), Find the minimum distance code length, Dimension and generate the code word corresponding to any 2 message blocks of this RM code. (9)
- b) Discuss the decoding of Reed-Solomon code using Berlekamp's algorithm (5)

OR

- 16 a) Explain the method of encoding and decoding performed in RS code. (9)
- b) Obtain the generator vectors of RM (1,3) code (5)

Module IV

- 17 For a (2,1,2) convolutional encoder with generator sequences $g(1) = (1\ 1\ 1)$, $g(2) = (1\ 0\ 1)$. (14)
- i. Draw the binary encoder.**
 - ii. State table.**
 - iii. State transition table.**
 - iv. State diagram.**

v. Find the encoded sequence for the message 1 0 1 1 1.

OR

- 18 a) Explain turbo codes with and without puncturing. (5)
- b) For a (2,1,4) convolutional encoder with generator sequences (9)
- $g(1) = (0\ 1\ 1\ 1\ 1)$, $g(2) = (0\ 1\ 1\ 0\ 1)$, draw the encoder, compute the generator polynomial and find the output sequence produced by the information 1 0 1 1 1 using matrix method.

Module V

- 19 a) Explain the relationship between Tanner graph and the parity-check matrix (7)
- with an example. Define cycle for the Tanner graph of LDPC.
- b) Given the parity check matrix of an LDPC, decode the received data $r=[0\ ?\ ?\ 1\ 0\ ?\ 0]$. Assume that the channel is BEC. (7)

$$H = \begin{bmatrix} 1 & 1 & 0 & 1 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 & 0 & 1 & 0 \\ 1 & 1 & 1 & 1 & 0 & 0 & 1 \end{bmatrix}$$

OR

- 20 a) What are frozen bits? Explain the encoding method with suitable example. (7)
- b) Mention the applications of polar codes in 5G. (7)
